### ABSTRACT

Title of thesis:	FOVEATED RENDERING TECHNIQUES IN MODERN COMPUTER GRAPHICS
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Foveated rendering coupled with eye-tracking has the potential to dramatically accelerate interactive 3D graphics with minimal loss of perceptual detail. I have developed a new foveated rendering technique: Kernel Foveated Rendering (KFR), which parameterizes foveated rendering by embedding polynomial kernel functions in log-polar mapping. This GPU-driven technique uses parameterized foveation that mimics the distribution of photoreceptors in the human retina. I present a two-pass kernel foveated rendering pipeline that maps well onto modern GPUs. In the first pass, I compute the kernel log-polar transformation and render to a reduced-resolution buffer. In the second pass, I have carried out the inverse-log-polar transformation with anti-aliasing to map the reduced-resolution rendering to the full-resolution screen. I carry out user studies to empirically identify the KFR parameters and observe a 2.8X - 3.2X speedup in rendering on  $4K \ UHD$  (2160*p*) displays. The eye-tracking-guided kernel foveated rendering can resolve the mutually conflicting goals of interactive rendering and perceptual realism.

## FOVEATED RENDERING TECHNIQUE IN MODERN GRAPHICS

by

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Thesis submitted to the Faculty of the Graduate School of the University of Maryland, College Park in partial fulfillment of the requirements for the degree of Master of Science 2018

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### Chapter 1: Introduction

#### 1.1 Overview

Human vision spans a field of view of  $135^{\circ} \times 160^{\circ}$ , but the highest-resolution foveal vision covers only the central  $1.5^{\circ} \times 2^{\circ}$  [3]. Patney *et al.* [5] have estimated that in modern virtual reality head-mounted displays (HMD) only 4% of the pixels are mapped onto the fovea. Therefore, foveated rendering techniques that allocate more computational resources for foveal pixels and fewer resources elsewhere can dramatically speed up rendering [13] for large displays, especially for virtual and augmented reality headsets equipped with eye trackers.

Araujo and Dias [14] use a log-polar mapping to approximate the excitation of the cortex in the human vision system. The classic log-polar transformation has been used for foveating 2D images on the GPU [15]. However, to the best of my knowledge, direct use of the log-polar mapping for 3D graphics has not yet been attempted on GPUs.

In my thesis, I present a kernel foreated rendering pipeline for modern GPUs that parameterizes foreated rendering by embedding polynomial kernel functions in the classic log-polar mapping. This allows us to easily vary the sampling density and distribution, and match them to human perception in virtual reality HMDs. In contrast to adaptive sampling in Cartesian coordinates, which requires a complex interpolation process [10] and the classic three-pass foveated rendering pipeline [3], KFR just needs a two-pass algorithm. In the first pass, I carry out the kernel log-polar transformation and render to a reduced-resolution framebuffer using deferred shading [16,17]. In the second pass, I apply the inverse kernel log-polar transformation to the reduced-resolution framebuffer to map the final foveated rendering to the full-resolution display.

I have built several foreated renderings with varying sampling density and distribution and evaluate them via pilot and final user studies. I have found the optimal parameters with minimal perceptual errors that correspond to the distribution of photoreceptors in the retina. This algorithm is designed to achieve a high frame rate by shading fewer pixels in the peripheral vision. Finally, I have validated my approach on 3D rendering of textured meshes as well as ray-marching scenes.

The KFR pipeline is broadly applicable for eye-tracking devices, and efficiently testing, or previewing real-time rendering results with global lighting and physically based rendering.

In summary, my contributions include:

- 1. designing the kernel log-polar mapping algorithm to enable a parameterized trade-off of visual quality and rendering speed for foveated rendering,
- 2. conducting user studies to identify the kernel foreated rendering parameters governing the sampling distribution and density to maximize perceptual realism and minimize computation,

3. mapping kernel foreated rendering onto the GPU to achieve speedups of 2.8X for textured 3D meshes and 3.2X for ray-casting scenes for  $3840 \times 2160$  displays with minimal perceived loss of detail.

#### 1.2 Human Vision System

There is a large research literature that documents the falloff of accuracy in visual periphery. Most of the previous research on foreated perception has been surveyed in [18]. Recent research has also addressed the issue of perception time for depicting information in the far peripheral field [19].

A commonly used model is the *linear acuity model*, which measures the minimum angle of resolution (MAR). A linear model matches both anatomical data and is applicable for many low-level vision tasks [18]. However, the model only works for the "central" vision (with angular radius  $\leq 8^{\circ}$ ), after which MAR rises more steeply [3]. In the periphery, receptors become increasingly sparse relative to the eyes' optical system Nyquist limit.

Another model is the *log acuity model*. It has been found that the excitation of the cortex can be approximated by a log-polar mapping of the eye's retinal image [20]. The calculation of this model is cheap and fast, thus being used in many practical applications such as computer vision, robotics, and other fields.

Curcio [1,2] proposed the mixed acuity model. As shown in Figure 1.1, the Ganglion cell (orange) density tends to match the photoreceptor density in the fovea (left), but many photoreceptors map to the same Ganglion cell away from the fovea.



Figure 1.1: Spatial distribution of various retinal components, using data from [1] and [2]. Ganglion cell (orange) density tends to match photoreceptor density in the fovea (left), but away from the fovea many photoreceptors map to the same Ganglion cell. 'Nasal', 'Temp', 'Sup' and 'Inf' indicate the four directions (nasal, temporal, superior, inferior) away from the fovea.

'Nasal', 'Temp', 'Sup' and 'Inf' indicate the four directions (nasal, temporal, superior, inferior) away from the fovea.

Most of the foveated rendering algorithms are inspired by the acuity models mentioned above. However, it is not easy to quantify the pixel density rate by using the models mentioned above. Previous research has addressed the issue of adjusting visual acuity by conducting user studies with eye tracking technologies.

Kortum *et al.* [21] invented a foveated imaging system and validate their system using eye tracking. Minimal perceptual artifacts are reported with bandwidth reductions of up to 94.7%. Guenter *et al.* [3] conducted user study by letting the users compare the foveated image and non-foveated image. They found a more aggressive mean threshold and a more conservative threshold, which achieved speedups of 5.7 and 4.8 compared to non-foveated rendering. Patney *et al.* [6] conducted user study by fitting a psychometric function to the user performance for different shading strategies, and found a satisfactory shading rate which provides the most speedup.

#### 1.3 Foveation Techniques

#### 1.3.1 Foveated Images and Videos

The last few decades have seen significant advances in foreated rendering for 2D images and videos.

Burt [22] has generated foreated images with multi-resolution Gaussian pyramids. He takes advantage of a coarse-to-fine scheme to adaptively select the critical information for constructing the foreated image. Kortum and Geisler [21] have developed one of the earliest eye-tracking-based foreated imaging systems with space-variant degradation. The structure of their image foreation system is shown in Figure 1.2. Using  $256 \times 256$  8-bit gray-scale images, they have achieved bandwidth reduction of up to 94.7% with minimal perceptual artifacts. Other image foreation techniques include embedded zero-tree wavelets [23], set partitioning in hierarchical trees [24], wavelet-based image foreation [25], embedded foreation image coding [26], and gigapixel displays [27].



Figure 1.2: General flow diagram of the operation of the foveated imaging system.

Video foveation has also been explored [28-30]. The filter bank method is used for video preprocessing before using standard video compression algorithms (*e.g. MPEG and H.26x*) [29, 31, 32]. Foveation filtering has been implemented with the quantization processes in standard MPEG and H.26x compression [33, 34]. Video foveation coupled with eye tracking could reduce overall system latency, including network latency, processing latency, and display latency [35]. An overview of video foveation is shown in Figure 1.3.



Figure 1.3: Overview of the envisioned end-to-end architecture for supporting gazeaware streaming solutions for VR.

While previous work in foveation for images and videos provides strong foundations, most of these methods cannot be easily generalized for interactive 3D graphics rendering on modern GPUs. A notable exception is the work by Antonelli *et al.* [15], which uses log-polar mapping to speed-up 2D image rendering on modern GPUs. However, their approach does not directly work with 3D graphics primitives and does not use kernel functions.

### 1.3.2 Foveated 3D Graphics

Weier *et al.* [36] have reviewed several approaches for foveated rendering including mesh simplification in the areas of lower acuity [37–39]. However, these days shading has often been found to dominate the cost for rendering sophisticated scenes on modern graphics pipelines [4, 8].

Ragan-Kelley et al. [40] use decoupled sampling for stochastic super-sampling

of motion and defocus blur at a reduced shading cost. Guenter *et al.* [3] present a three-pass pipeline for foveated 3D rendering by using three eccentricity layers around the tracked gaze point. As shown in Figure 1.4, the innermost layer is rendered at the highest resolution (native display), while the successively outer peripheral layers are rendered with progressively lower resolution and coarser level of detail (LOD). They interpolate and blend between the layers and use frame jitter and temporal re-projection to reduce spatial and temporal artifacts. However, this approach renders the scene three times, which requires lots of rendering resources.

Vaidyanathan *et al.* [4] present a novel approach using a generalization of multi-sample anti-aliasing (MSAA). They perform foreated rendering by sampling coarse pixels ( $2 \times 2$  pixels and  $4 \times 4$  pixels) in the peripheral regions as shown in Figure 1.5. This approach targets small-form-factor devices with high resolution, such as phones and tablets rather than HMDs. It therefore presents two challenges for HMDs: the effective pixel size in current HMDs is too large for MSAA, and gaze-dependent motions exaggerate the artifacts.

Patney *et al.* [5,6] address temporal artifacts in foreated rendering by using pre-filters and temporal anti-aliasing. Because human eyes are sensitive to edges, they add contrast preservation for the foreated image, which greatly enhances the image quality by reducing the tunneling effect as shown in Figure 1.6. They tested the foreated rendering effect on both Desktop and VR headset.

Clarberg *et al.* [7] propose a modification to the current hardware architecture, which enables flexible control of shading rates and automatic shading reuse between triangles in tessellated primitives as shown in Figure 1.7.



Figure 1.4: Guenter *et al.* [3] render three eccentricity layers (red border = inner layer, green = middle layer, blue = outer layer) around the tracked gaze point (pink dot), shown at their correct relative sizes in the top row. These are interpolated to native display resolution and smoothly composited to yield the final image at the bottom. Foveated rendering greatly reduces the number of pixels shaded and overall graphics computation.



Figure 1.5: Vaidyanathan *et al.* [4] perform for for a rendering by sampling coarse pixels  $(2 \times 2 \text{ pixels and } 4 \times 4 \text{ pixels})$  in the peripheral regions.



Figure 1.6: Patney *et al.* [5,6] perform foreated rendering by sampling coarse pixels and address temporal artifacts in foreated rendering by using pre-filters and temporal anti-aliasing.



Figure 1.7: Clarberg *et al.* [7] have proposed an approach in which pixel shading is tied to the coarse input patches and reused between triangles, effectively decoupling the shading cost from the tessellation level, as shown in this example.

He *et al.* [8] introduce multi-rate GPU shading to support more shading samples near regions of specular highlights, shadows, edges, and motion blur regions, helping achieve a 3X to 5X speedup as shown in Figure 1.8. However, this implementation of multi-rate shading requires an extension of the graphics pipeline, which is not available on commodity graphics hardware.



Figure 1.8: He *et al.* [8] introduce multi-rate GPU shading to support more shading samples near regions of specular highlights, shadows, edges, and motion blur regions, helping achieve a 3X to 5X speedup.

Swafford *et al.* [9] implement four foveated renderers as shown in Figure 1.9. The first method reduces the effective rendered pixel density of the peripheral region while maintaining the base density of the foveal window, as shown in Figure 1.9(a). The second varies per-pixel depth-buffer samples in the fovea and periphery for screen-space ambient occlusion. Although a very low number of per-pixel samples can cause banding, they expect these differences to go unnoticed in the periphery due to the loss of visual acuity and contrast sensitivity, as shown in Figure 1.9 (b). The third method normally casts rays to geometry and detects intersections with a given number of depth layers, represented as a series of RGBA textures mapped on the geometry, then it varies the per-pixel ray-casting steps across the field of view, as shown in Figure 1.9 (c). The final method implements a terrain renderer using GPU-level tessellation for the fovea. In order to determine the appropriate level of tessellation, we project the foveal window from screen coordinates into the scene. If a tile falls within either the foveal or peripheral field of view, the level of tessellation is set statically to the appropriate level. If the tile falls between the two regions (on the blending border) the level of tessellation is linearly interpolated between the two levels, as shown in Figure 1.9 (d).

Stengel *et al.* [10] use adaptive sampling from fovea to peripheral regions in a gaze-contingent rendering pipeline as shown in Figure 1.10. To compensate for the missing pixels caused by sparsely distributed shading samples on the periphery, they use pull-push [41] interpolation to create the full foveated image. This strategy achieves a reduction of rendertime of 25.4% (with speedup of 1.3X) and reduction of shading time of 41% (with speedup of 1.7X).

Sun *et al.* [11] design a real-time foreated 4D light field rendering and display system as shown in Figure 1.11. Their prototype renders only 16% - 30% of the rays



Figure 1.9: Swafford *et al.* [9] implement four foveated renderers as described in the text of the figure. (a) is the Annotated view of a foveated resolution render with moderate settings precomposition. The checkerboard area represents the proportion of pixels saved for the targeted simulated resolution; (b) is the strips from two foveated renders with the same fixation point (bottom-right) but different peripheral sampling levels. Region transition is handled smoothly, but at four samples there are noticeable artifacts in the peripheral region, such as banding; (c) Top: Sample frame from our ray-casting method with 120 per-pixel steps in the foveal region (within circle) and 10 per-pixel steps in the peripheral region (outwith circle). Bottom: Close-up ofright lamp showing artifacts across different quality levels; (d) is the Wireframe view of our foveated tessellation method. The inner circle is the foveal region, between circles is the inter-regional blending, and outside the circles is the peripheral region.



Figure 1.10: Stengel *et al.* [10] use adaptive sampling from fovea to peripheral regions in a gaze-contingent rendering pipeline and compensate for the missing pixels by pull-push interpolation.

without compromising the perceptual quality.

Recently, deferred shading has been used for antialiasing foveated rendering. Karis [42] optimizes temporal anti-aliasing for deferred shading, which uses samples over multiple frames to reduce flickering. Crassin *et al.* [43] reduce aliasing by prefiltering sub-pixel geometric detail in the G-buffer for deferred shading. Chajdas *et al.* [44]'s subpixel anti-aliasing operates as a post-process on a rendered image with super-resolution depth and normal buffers. It targets deferred shading renderers that cannot use MSAA.

In this thesis, we present a simple two-pass foreated rendering pipeline that maps well onto modern GPUs. Kernel foreated rendering (KFR) provides gradually changing resolution and achieves 2.8X - 3.2X speedup with little perceptual loss.



Figure 1.11: Sun *et al.* [11] design a real-time foveated 4D light field rendering and display system.

### 1.4 Eye Tracking

Eye tracking has been used in graphics for a number of applications, including validation of mesh saliency [45]. As the visual complexity rises in virtual worlds [46–48], biomedical datasets [49–51], and large images [52, 53], the need for eye-tracking to rapidly identify areas of interest and selectively render them at greater detail will also increase.

Eye tracking in VR is implemented by adding a series of infrared emitters and sensors embedded around the headset's lenses as shown in Figure 1.12. The headset uses the images collected by the sensors to calculate the position and direction of gaze for both eyes.

The development of eye-tracking technology makes foreated rendering possible. FOVE has released a foreated rendering headset with eye tracking in 2017. HTC Vive and Qualcomm are collaborating with Tobii in the development of an eye tracking VR headset.

Latency is one of the most important system components for eye tracking. According to Albert *et al.* [54], an extra eye tracking latency of 80 - 150 ms causes a significant reduction in acceptable amount of foveation, but a similar decrease in acceptable foveation was not found for shorter eye-tracking latencies of 20 ms 40 ms, suggesting that a total system latency of 50 ms to 70 ms could be tolerated.



Figure 1.12: Tobii eye-tracker in a HTC Vive VR headset.

### Chapter 2: Kernel Foveated Rendering

### 2.1 Overview

Overall, my algorithm applies the kernel log-polar transformation for rasterization in a reduced-resolution log-polar buffer (LP-buffer), carries out shading within the LP-buffer, and then uses the inverse kernel log-polar transformation to render on the full resolution display. This is shown in Figure 1.13.

In the classic log-polar transformation [15], given a  $W \times H$  pixel display screen, and an LP-buffer of  $w \times h$  pixels, the screen-space pixel (x, y) in Cartesian coordinates is transformed to (u, v) in the log-polar coordinates according to Equation 2.1,

$$u = \frac{\log \|x', y'\|_2}{L} \cdot w$$

$$v = \frac{\arctan\left(\frac{y'}{x'}\right)}{2\pi} \cdot h + \mathbf{1} [y' < 0] \cdot h$$
(2.1)

where, (x', y') represent (x, y) with respect to the center of the screen as origin, L is the log-distance from the center to the corner of the screen, and  $\mathbf{1}[\cdot]$  is the indicator function,

$$x' = x - \frac{W}{2}, \quad y' = y - \frac{H}{2}, \quad L = \log\left(\left\|\frac{W}{2}, \frac{H}{2}\right\|_{2}\right)$$
 (2.2)



Figure 1.13: An overview of the KFR pipeline. I transform the necessary parameters and textures in the G-buffer from Cartesian coordinates to log-polar coordinates, compute lighting in the log-polar (LP) buffer and perform internal anti-aliasing. Next, I apply the inverse transformation to recover the framebuffer in Cartesian coordinates and employ post anti-aliasing to reduce the foveation artifacts.



Figure 1.14: Transformation from Cartesian coordinates to log-polar coordinates with kernel function  $\mathbf{K}(x) = x^{\alpha}$ . (a) is the image in the Cartesian coordinates, (b)–(e) are the corresponding images in the log-polar coordinates with varying kernel parameter  $\alpha$ . Matching colors in the log-polar and Cartesian coordinates show the same regions.



Figure 1.15: Comparison of foreated frame with different  $\alpha$  (forea is marked as the semi-transparent ring in the zoomed-in view): (a) original scene, (b) foreated with  $\alpha = 1.0$ , (c) foreated with  $\alpha = 4.0$ , (d) foreated with  $\alpha = 5.0$ , and (e) foreated with  $\alpha = 6.0$ . The lower zoomed-in views show that large  $\alpha$  enhances the peripheral detail; the upper zoomed-in views show that when  $\alpha \geq 5.0$ , foreal quality suffers.

$$\mathbf{1}\left[y'<0\right] = \begin{cases} 1 & , y'<0\\ 0 & , y' \ge 0 \end{cases}$$
(2.3)

Notice how the central dark green area in Figure 1.14 (a) is mapped to a relatively large region in the left part of the log-polar coordinates in Figure 1.14 (b), while the peripheral regions of Figure 1.14 (a) are mapped to a relatively small part of Figure 1.14 (b).

In the inverse log-polar transformation, a pixel with log-polar coordinates (u, v)is transformed back to (x'', y'') in Cartesian coordinates. Let

$$A = \frac{L}{w}, \quad B = \frac{2\pi}{h}, \tag{2.4}$$



Figure 1.16: The relationship among  $\sigma^2$ ,  $\mathbf{K}(x) = x^{\alpha}$ , and the sampling rate. The number of samples in each image is proportional to  $\sigma^2$ . I use a variant of the PixelPie algorithm [12] to generate the Poisson samples shown.



Figure 1.17: Comparison of foveated rendering with varying  $\alpha$  for 2560 × 1440 resolution. From left to right: original rendering, kernel log-polar rendering, and the foveated rendering with zoomed-in view of the peripheral regions. Here  $\sigma = 1.8$ , (a) classic log-polar transformation, i.e.  $\alpha = 1.0$ , (b) kernel function with  $\alpha = 2.0$ , (c) kernel function with  $\alpha = 3.0$ , and (d) kernel function with  $\alpha = 4.0$ . The foveated rendering is at 67 FPS while the original is at 31 FPS.



Figure 1.18: Comparison of foveated rendering with varying  $\sigma$  for 2560 × 1440 resolution. From left to right: original rendering, kernel log-polar rendering, the recovered scene in Cartesian coordinates, and a zoomed-in view of peripheral regions. Here,  $\mathbf{K}(x) = x^4$ , (a) full-resolution rendered at 31 FPS, (b)  $\sigma = 1.2$  at 43 FPS, (c)  $\sigma = 1.8$  at 67 FPS, and (d)  $\sigma = 2.4$  at 83 FPS.

then the inverse transformation can be formulated as Equation 2.5,

$$x'' = \exp(Au)\cos(Bv)$$

$$y'' = \exp(Au)\sin(Bv)$$
(2.5)

To understand how the resolution changes in the log-polar space, consider  $r = \|x,y\|_2 = \exp{(Au)}.$ 

Now, dr represents the change in r based on u,

$$\mathrm{d}r = A \cdot \exp\left(Au\right) \mathrm{d}u. \tag{2.6}$$

Inversely,  $\mathscr{D}$  is defined as the number of pixels in the LP-buffer that map to a single pixel on the screen,

$$\mathscr{D} = \frac{\mathrm{d}u}{\mathrm{d}r} = \frac{1}{A} \cdot \exp(-Au). \tag{2.7}$$

Equation 2.7 shows the foveation effect of pixel density decreasing from the fovea to the periphery. In this formulation, it is not easy to systematically alter the density fall-off function and evaluate the perceptual quality of foveated rendering.

I propose a kernel log-polar mapping algorithm that allows us more flexibility to better mimic the fall-off of photo-receptor density of the human visual system,

$$\mathscr{D} = \frac{\exp\left(-wC\sigma \cdot \mathbf{K}^{-1}\left(\frac{u}{w}\right)\right)}{C\sigma \cdot \mathbf{K}^{-1'}\left(\frac{u}{w}\right)}.$$
(2.8)

Here, the constant parameter  $C = \sqrt{1 + \left(\frac{H}{W}\right)^2}$  represents the ratio between screen diagonal and screen width.  $\sigma = \frac{W}{w}$  represents the ratio between the fullresolution screen width and the reduced-resolution LP-buffer width,  $\sigma^2 = \frac{W^2}{w^2}$  represents the ratio between the number of pixels in the full-resolution screen and the number of pixels in the reduced-resolution LP-buffer. Larger  $\sigma^2$  corresponds to more condensed LP-buffer, which means less calculation in the rendering process. A more condensed LP-buffer also means more foreation and greater peripheral blur.

The kernel function  $\mathbf{K}(x)$  can be any monotonically increasing function with  $\mathbf{K}(0) = 0$  and  $\mathbf{K}(1) = 1$ , such as the sum of power functions,

$$\mathbf{K}(x) = \sum_{i=0}^{\infty} \beta_i x^i, \quad \text{where } \sum_{i=0}^{\infty} \beta_i = 1.$$
(2.9)

Such kernel functions can be used to adjust the pixel density distribution in the LP-buffer. I use  $\mathbf{K}(x) = \sum_{i=0}^{\infty} \beta_i x^i$  in this thesis because the calculation of power functions is fast on modern GPUs. There may be other kernel functions worth trying, such as  $\mathbf{K}(x) = \sin(x \cdot \frac{\pi}{2})$  and  $\mathbf{K}(x) = \frac{e^x - 1}{e^{-1}}$ . For example, for  $C = \sqrt{2}$  and  $\mathbf{K}(x) = x^{\alpha}$ , the relationship between  $\mathscr{D}$  and r under varying  $\sigma^2$  and  $\alpha$  is illustrated in Figure 1.16<sup>-1</sup>. Kernel functions can adjust the pixel density such that the percentage of the peripheral regions in the LP-buffer increases as shown in Figure 1.14 (c), (d), and (e). This makes it possible to increase the peripheral image quality while maintaining the same frame rates. A comparison among different kernel functions is shown in Figure 1.17 with  $\sigma = 1.8$  and  $C = \sqrt{2}$ . The use of the kernel function reduces the artifacts in the zoomed-in peripheral view, improving the peripheral image quality. Meanwhile, as shown in Figure 1.15, when  $\alpha \geq 5.0$ , the sampling rate of even the foreal region drops, affecting the visual quality of the forea. A comparison among different  $\sigma$  is shown in Figure 1.18 with fixed  $\alpha = 4.0$ ,  $C = \sqrt{2}$ .

<sup>&</sup>lt;sup>1</sup>The figure is the visualization of sampling rate rather than the true sampling map.

### 2.2 Pass 1: Forward Kernel Log-polar Transformation

### 2.2.1 Kernel Log-polar Transformation

For each pixel in screen space with coordinates (x, y), foveal point  $\mathbf{F}(\mathring{x}, \mathring{y})$  in Cartesian coordinates, I change Equation 2.1 to Equation 2.10,

$$u = \mathbf{K}^{-1} \left( \frac{\log \|x', y'\|_2}{L} \right) \cdot w$$

$$v = \left( \arctan\left(\frac{y'}{x'}\right) + \mathbf{1} \left[y' < 0\right] \cdot 2\pi \right) \cdot \frac{h}{2\pi}$$
(2.10)

Here,

$$x' = x - \mathring{x}, \quad y' = y - \mathring{y}.$$
 (2.11)

 $\mathbf{K}^{-1}(\cdot)$  is the inverse of the kernel function, and L is the log of the maximum distance from fovea to one of the four corners of the screen as shown in Equation 2.12,

$$L = \log\left(\max\left(\max\left(l_1, l_2\right), \max\left(l_3, l_4\right)\right)\right).$$
(2.12)

Here,

$$l_{1} = \|\dot{x}, \dot{y}\|_{2}$$

$$l_{2} = \|W - \dot{x}, H - \dot{y}\|_{2}$$

$$l_{3} = \|\dot{x}, H - \dot{y}\|_{2}$$

$$l_{4} = \|W - \dot{x}, \dot{y}\|_{2}$$
(2.13)

### 2.2.2 Lighting

In lighting calculation for traditional deferred shading, mesh positions, normals, depth and material information such as roughness, index of reflection, and normal

### ALGORITHM 1: Kernel Log-polar Transformation Input:

Fovea coordinates in screen space:  $(\mathring{x}, \mathring{y})$ ,

pixel coordinates in screen space: (x, y).

#### Output:

Pixel coordinates in the log-polar space: (u, v).

- 1: acquire fovea coordinates  $(\mathring{x}, \mathring{y})$
- 2: for  $x \in [0, W]$  do
- 3: **for**  $y \in [0, H]$  **do**
- 4:  $x' = x \mathring{x}$
- 5:  $y' = y \mathring{y}$
- 6:  $u = \mathbf{K}^{-1} \left( \frac{\log \|x', y'\|}{L} \right) \cdot w$ 7:  $v = \left( \arctan \left( \frac{y'}{x'} \right) + \mathbf{1} \left[ y' < 0 \right] \cdot 2\pi \right) \cdot \frac{h}{2\pi}$
- 8: end for
- 9: end for

maps are fetched from the G-buffer [16, 17]. Instead of obtaining information from the G-buffer with texture coordinates (x, y), in my approach, I sample from the transformed kernel log-polar texture coordinates (u, v). The reduced-resolution of the log-polar (LP) buffer helps in reducing the lighting calculation to only those pixels that matter in the final foreated rendering.

### 2.2.3 Internal Anti-aliasing

Due to the low-resolution of the LP-buffer, there may be artifacts in the peripheral regions after the inverse transformation. However, I can directly perform denoising in the log-polar space. To reduce artifacts in the peripheral regions, I use a Gaussian filter with a  $3 \times 3$  kernel for the right part of the texture (corresponding to the peripheral regions) in the LP-buffer. Since the LP-buffer pixels correspond to the adaptive detail of foreated rendering, the Gaussian filtering in the LP-buffer gives us higher-level of anti-aliasing in the peripheral regions.

#### 2.3 Pass II: Inverse Kernel Log-Polar Transformation

Pass II performs the inverse kernel log-polar transformation to Cartesian coordinates, applies anti-aliasing, and renders to screen.

### 2.3.1 Inverse Kernel Log-polar Mapping Transformation

I can recover the Cartesian coordinates (x'', y''), from the pixel coordinates (u, v) and the fovea coordinates  $(\mathring{x}, \mathring{y})$  using Algorithm 2.

### 2.3.2 Post Anti-aliasing

One of the crucial considerations in foveated rendering is mitigating temporal artifacts due to aliasing in the peripheral, high eccentricity regions. I apply temporal anti-aliasing (TAA) [42] with Halton sampling [55] to the recovered screen-space pixels after the inverse kernel log-polar transformation. I also use Gaussian filtering with different kernel sizes  $\eta$  for different L (as defined in Equation 2.12) in post anti-aliasing. The kernel size  $\eta$  is shown in Equation 2.14, which depends on the normalized distance between the pixel coordinate and the fovea,

$$\eta = 3 + 2 \times \left[ \frac{\frac{\|x', y'\|_2}{e^L} - 0.10}{0.05} \right].$$
(2.14)

### ALGORITHM 2: Kernel Log-polar Inverse Transformation Input:

Fovea coordinates in screen space:  $(\mathring{x}, \mathring{y})$ ,

pixel coordinates in the log-polar coordinates: (u, v).

#### **Output:**

Screen-space coordinates (x'', y'') for pixel coordinates (u, v).

- 1: update L with fovea coordinates  $(\mathring{x}, \mathring{y})$  with Equation 2.12
- 2: let  $A = \frac{L}{w}, B = \frac{2\pi}{h}$
- 3: for  $u \in [0, w]$  do
- 4: **for**  $v \in [0, h]$  **do**
- 5:  $x'' = \exp\left(A \cdot \mathbf{K}\left(u\right)\right) \cdot \cos\left(Bv\right) + \mathring{x}$
- 6:  $y'' = \exp\left(A \cdot \mathbf{K}\left(u\right)\right) \cdot \sin\left(Bv\right) + \mathring{y}$
- 7: end for
- 8: end for

# Chapter 3: User Study

I have carried out user studies to empirically establish the most suitable foveation parameter values for  $\sigma$  and  $\alpha$  that result in visually acceptable foveated rendering. To systematically investigate this, I conducted a pilot study to examine a broad range of the two parameters,  $\sigma^2$  and  $\alpha$ . I used the results and my experience with the pilot study to fine tune the protocol and ranges of  $\sigma^2$  and  $\alpha$  for the final user study.



Figure 2.1: User study setup.



Figure 2.2: The percentage of times that the participants considered the foveated rendering and the full-resolution rendering to be the same for varying  $\sigma^2$  and  $\alpha$  in pilot user study with 24 participants.

#### 3.1 Apparatus

My user study apparatus, shown in Figure 2.1, consists of an *Alienware* laptop with an *NVIDIA GeForce GTX 1080*, a *FOVE* head-mounted display, and an *XBOX* controller. The *FOVE* display has a 100° field of view, a resolution of  $2560 \times 1440$ , and a 120 Hz infrared eye-tracking system with a precision of 1° and a latency of 14 ms, the system latency meets the eye tracking delay requirement of 50 ms - 70 ms.

#### 3.2 Pilot Study

#### 3.2.1 Procedure

The session for each participant lasted between 35 - 50 minutes and involved four stages: introduction, calibration, training, and testing.



Identical percentage under different  $\alpha$  and  $\sigma$ 

Figure 2.3: The percentage of times that participants considered the foveated rendering and the full-resolution rendering to be identical for different  $\sigma^2$  and  $\alpha$  in the final user study with 18 participants.

In the introduction stage, I showed participants the *FOVE* headset, the eye trackers, and the *XBOX* controllers and discussed how to use them. I did not provide any information about the research or the algorithm to avoid biasing the participants towards any rendering.

After the participant comfortably wore the HMD, I moved forward to the calibration stage, where I ran a one-minute eye-tracking calibration program provided by the *FOVE* software development kit.

In the training stage, I presented the participants with 20 trials with different

combinations of  $\sigma^2$  and  $\alpha$ , to ensure that they are familiar with the HMD and the controller.

Trials in the training and testing stages were identical. In each trial of the two-alternative forced choice test, I presented participants with a pair of rendered scenes, each for 2 seconds and separated by a black-screen interval of 0.75 seconds. One scene uses full-resolution rendering, and the other uses KFR with different parameters  $\sigma^2$  and  $\alpha$ . In each trial, I presented the KFR scene and the full-resolution scene in a random order. The participant indicated whether the two images look the same by pressing a button on the *XBOX* controller. I instructed the participants to maintain their gaze at the center of the screen, even though the foreated renderer can use eye-tracking to update the foreated image.

The testing stage had three sessions, each with 56 trials. The LP-buffer resolution reduction parameter  $\sigma$  ranges from 1.0 to 3.6 with step size 0.2 ( $\sigma^2$  ranges from 1.00 to 12.96), and the kernel sampling distribution parameter  $\alpha$  ranges from 1 to 4 with step size 1. I rendered scenes from the *Sponza* and *Amazon Lumberyard Bistro* datasets for different sessions. I allowed the participants to have some rest between different sessions.

### 3.2.2 Participants

In the pilot study, I recruited 24 participants via campus email lists and flyers. All participants are at least 18 years old with normal or corrected-to-normal vision (with contact lenses). The participants are collected using campus flyers and emails.

#### 3.2.3 Results and Analysis

I define  $P_I$  as the percentage of the trials for which participants reported the two images shown in a trial to be the same. The results of  $P_I$  are shown in Figure 2.2. First, I find that  $P_I$  is inversely related to  $\sigma^2$ . With increase in  $\sigma^2$ , the LP-buffer gets smaller, thus reducing the overall sampling rate in foveated rendering. Second, I notice that with the increase of  $\alpha$ ,  $P_I$  significantly increases for  $\sigma$  ranging from 1.2 to 2.8 ( $\sigma^2$  ranging from 1.44 to 7.84). This shows that for the same  $\sigma$ , the perception of the quality of foveated rendering increases by the use of  $\alpha$  for kernel functions. For  $\sigma = 1.0$  and  $\sigma > 2.8$  the improvement is not significant. The reason is that for  $\sigma = 1.0$ , the foveated renderings for  $\alpha = 1$  and  $\alpha > 1$  are both clear, there is little space for improvement. Similarly, for  $\sigma > 2.8$ , even if the quality improves by applying kernel functions, it still looks blurry for both images. Therefore, the participants choose "different" for these comparisons. Third, some participants reported that the length of the study led to visual fatigue and that they were not sure about some of their responses.

Using the above observations, I modified the final user study to be shorter and more focused.

First, to reduce the total time that participants are in the HMD, I used the fact that most participants found foreated renderings different from the full-resolution rendering for  $\sigma > 2.4$  ( $\sigma^2 > 5.76$ ). Since the goal is to accelerate rendering while maintaining perceptually similar quality, I reduced the range of  $\sigma$  to be between 1.2 to 2.4 ( $\sigma^2$  between 1.44 to 5.76) in the final user study. Second, I observed that the participants quickly came up to speed within a couple of trials in the training session. I therefore reduced the number of trials in the training session from 20 to 5. This also allowed us to shorten the user study duration and maintain a high level of visual attentiveness of the participants. Third, some of the participants reported that the rendering time of 2 seconds was too short. To address this I increased the time of each rendering to 2.5 seconds in the final study. Fourth, to continually check for the visual attentiveness of the participants, I modified the final user study by randomly inserting 30% of the trials to be "validation trials" that had identical full-resolution renderings for both choices. If the participant declared these validation renderings to be different, I would ask the participant to stop, get some rest, and then continue. After making these changes, the total time participants spent in the HMD was reduced from around 25 minutes in the pilot study to around 15 minutes in the final study.

### 3.3 Final User Study

#### 3.3.1 Procedure

The introduction and calibration stages are the same as the pilot user study. The training session includes five trials with different parameters. Each testing session involves 28 trials with multiple parameter combinations (parameter  $\sigma$  ranging from 1.2 to 2.4 with the step size 0.2 ( $\sigma^2$  ranging from 1.44 to 5.76); and kernel parameter  $\alpha$  ranging from 1 to 4 with the step size 1) as well as additional "validation trials". Order of the parameters is fully counterbalanced. The participants are asked to rest after each session or if they do not pass a "validation trial". I also changed the rendering-display time to 2.5 seconds.

#### 3.3.2 Participants

I recruited 18 participants via campus email lists and flyers. All participants were at least 18 years old with normal or corrected-to-normal vision (with contact lenses). The participants are collected using campus flyers and emails.

#### 3.3.3 Results and Analysis

I report the percentage  $P_I$  and the corresponding standard error in Figure 2.3. I make the null hypothesis  $(H_0)$  that the foveated rendering results with the four kernel functions are equally effective. As shown in Table 1, with a Cochran's Q test [56,57], I have found that there exists a significant difference across the multiple  $\alpha$  for  $\sigma = 1.6, 1.8, 2.2$  ( $\sigma^2 = 2.56, 3.24, 4.84$ ) with  $\chi^2(3) = 7.81, p < 0.05$ . The results with very small  $\sigma = 1.2, 1.4$  ( $\sigma^2 = 1.44, 1.96$ ) and very large  $\sigma = 2.4$  ( $\sigma^2 = 5.76$ ) are not significantly different, which are reasonable. For small  $\sigma^2$ , the rendering result without kernel function is clear enough, so there is little room for improvement. For large  $\sigma^2$ , both the rendering results with and without kernel function are blurry for the users.

To achieve visually acceptable results for foreated rendering, I use a threshold of 80% responses considering foreated rendering to be visually indistinguishable from full-resolution rendering. To achieve the highest rendering acceleration, I look for

Table 3.1: Cochrans Q values at different $\sigma^2$ .							
$\sigma^2$	1.44	1.96	2.56	3.24	4.00	4.84	5.76
Cochrans Q value	1.72	5.79	8.20	8.25	7.49	14.27	5.48
p value	0.631	0.122	0.042	0.041	0.058	0.002	0.139

the highest  $\sigma$  that met this threshold. I therefore choose  $\sigma = 1.8$  ( $\sigma^2 = 3.24$ ) and  $\alpha = 4$  as the desired parameters for the interactive rendering evaluation.

### Chapter 4: Rendering Acceleration

I implemented kernel foveated rendering on NVIDIA GeForce GTX 1080, by using the deferred shading pipeline of the Falcor engine [58]. I report results of my rendering acceleration for resolutions of  $1920 \times 1080$ ,  $2560 \times 1440$ , and  $3840 \times 2160$ . Using the results from the final user study, I selected the LP-buffer parameter  $\sigma = 1.8$ , and kernel parameter  $\alpha = 4$  for the evaluations below.

### 4.0.1 3D Textured Meshes

I use the Amazon Lumberyard Bistro [59] scene with physically-based shading, reflection, refraction, and shadows to simulate the complex shading effects as shown in Figure 4.1. I choose Amazon Lumberyard Bistro because this scene has complex triangular meshes, rendering textures and compact lighting effect. The comparison of the break-down of rendering time between KFR and the ground truth of deferred shading is shown in Table 2. I observed that the frame rate increases for all resolutions as shown in Table 3, with a speedup of 2.0X - 2.8X.

### 4.0.2 Ray-casting Rendering

Ray casting uses raysurface intersection tests to solve a variety of problems in computer graphics and computational geometry. It can also be used for creating scenes. Rendering of high-resolution ray cast scenes can be an extremely timeconsuming process. I used the complex ray-casting scene with 16 different primitives by Íñigo Quílez to evaluate the acceleration of kernel foreated rendering. Figure 4.2 shows a comparison of the foreated scene and the ground truth. The frame rate increases for all resolutions as shown in Table 3, with a speedup of 2.9X - 3.2X.



Figure 4.1: Comparison of (a) full-resolution rendering and (b) foveated rendering for 3D meshes involving a geometry pass with 1,020,895 triangles as well as multiple G-buffers at  $2560 \times 1440$  resolution.



Figure 4.2: Comparison of (a) full-resolution rendering and (b) foveated ray-marching scene with 16 samples per pixel rendered at  $2560 \times 1440$ .

Table 4.1: Timing comparison between the ground truth and KFR for one frame. The resolution is  $1920 \times 1080$ .

Procedure	Timing $(ms)$			
	Ground Truth	KFR		
Depth Pass	0.327	0.309		
Shadow Pass	3.744	4.503		
Defer Pass	2.985	3.034		
SkyBox	0.039	0.039		
Shading / Pass1	22.043	6.674		
Pass2	N/A	0.090		
Total	29.138	14.649		
Total GPU Time	31.892	17.052		

Table 4.2: Frame rate and speedup comparison for kernel foveated rendering at

Scene	3D Tex	tured Mesh	es	Ray	v Casting	
Resolution	Ground Truth	und Truth Foveated Speedup		Ground Truth	Foveated	Speedup
$1920 \times 1080$	$55 \ \mathrm{FPS}$	110 FPS	2.0X	20 FPS	$57 \; \mathrm{FPS}$	2.9X
$2560 \times 1440$	$31 \ \mathrm{FPS}$	$67 \; \mathrm{FPS}$	2.2X	$10 \ \mathrm{FPS}$	$30 \; \mathrm{FPS}$	3.0X
$3840 \times 2160$	8 FPS	$23 \ \mathrm{FPS}$	2.8X	5 FPS	$16 \; \mathrm{FPS}$	3.2X

different resolutions with  $\sigma = 1.8$ ,  $\alpha = 4.0$ .

### Chapter 5: Discussion and Limitations

#### 5.1 Discussion

Here I compare the Kernel Foveated Rendering (KFR) pipeline with selected prior art, including: *Foveated 3D Graphics* (F3D) [3], *Multi-rate Shading* (MRS) [8], *Coarse Pixel Shading* (CPS) [4], and *Adaptive Image-Space sampling* (AIS) [10].

As mentioned by [10], both MRS and CPS pipelines require adaptive shading features which are not yet commonly available on commodity GPUs and so they rely on software simulator implementations. In contrast, F3D, AIS, and the KFR pipelines can be easily mapped onto the current generation of GPUs.

The F3D pipeline has achieved impressive speedups of 10X-15X in the informal user study, and a factor of 4.8X - 5.7X in the formal user study. Nevertheless, the F3D approach uses three discrete layers, while the KFR parameterizes the distribution of samples continuously in the log-polar domain. F3D relies on specifically designed anti-aliasing algorithms including jitter sampling and temporal reprojection, thus limiting F3D to simpler material models and less complex geometry [10]. In contrast, KFR could easily be coupled with the state-of-the-art screen-space anti-aliasing techniques, such as TAA [42] and recent G-buffer anti-aliasing strategies [43].

Both the AIS and KFR pipelines mimic the continuously changing distribution



Figure 4.3: Temporal flickering issue. The original scene and the foveated scene of two consecutive frames ( $F_I$  and  $F_{II}$ ). In  $F_I$ , the specular reflection in the original scene as shown in the red and blue circles in the zoomed-in view of (a) are amplified in the foveated scene as shown in the zoomed-in view of (b). In the next frame  $F_{II}$ , the specular reflection in the original scene as shown in the pink circle in the zoomed-in view of (c) is amplified in the foveated scene as shown in the zoomed-in view of (d).

of photo-receptors in the retina. Nonetheless, there are three significant differences: complexity and evaluation of the perceptual model, interpolation, and speedup. First, AIS uses four parameters from [60] to approximately model the linear degradation behavior of acuity with 30° eccentricity. However, these parameters have not yet been evaluated on how they affect foreation and perception in HMDs or beyond  $30^{\circ}$ eccentricity. In contrast, KFR uses only two parameters: the reduced-resolution LPbuffer parameter  $\sigma$  and the kernel parameter  $\alpha$  in conjunction with a simple coordinate transformation. KFR has established desirable values of  $\alpha$  and  $\sigma$  through user studies in head-mounted displays. Second, AIS relies on the pull-push interpolation [41] to fill the pixels that are missed due to variable sampling of silhouette features and object saliency. In comparison, KFR uses the built-in GPU-driven mipmap interpolation which reduces the additional interpolation cost. However, it is worth investigating how incorporating object saliency [45, 61] could further improve the KFR pipeline. It is a challenge to compare multiple foveated approaches given the varying hardware and perceptual quality of the results. One possibility is to compare the speedups as percentages of rendering time reduction with certain reduction sampling rate. By rendering with 59% of the total amount of shaded pixels, AIS reports an overall rendering time reduction of 25.4%, while KFR achieves 29.9% reduction on average. Like AIS, KFR speedup also depends on the amount of time spent in shading; the greater the shader computations, the higher will be the KFR speedup.

#### 5.2 Limitations

Even though I have devised an efficient and effective foreated rendering pipeline, my system is not without some limitations.

### 5.2.1 Foveation Parameters

As discussed in Hsu *et al.* [62], the perceived quality of foveated rendering systems is highly dependent on the user and the scene. As the initial step towards kernel foveated rendering for 3D graphics, the user study in this thesis is only designed for selected static scenes. The foveation parameters may vary in dynamic scenes. Exploring the relationship between user demographic (*e.g.*, pupil size, contrast sensitivity, vision condition, and diopter) and display-dependent parameters of KFR is a potential future direction.

### 5.2.2 Temporal Flickering

In the post-processing stage, I have applied TAA to tackle the temporal flickering problem. However, in fly-through of the scene with glossy objects, I notice that view-dependent specular reflection changes before and after applying KFR. As shown in Figure 4.3, foreation amplifies the specular reflection regions, and makes the specular highlights flicker more.

## 5.2.3 Other Mapping Algorithms and Kernel Functions

KFR makes intuitive sense as the log-polar mapping has an initial resolution proportional to  $e^{-r}$ , and the kernel functions can fine tune this mapping. My choice of kernel functions is not unique; other mapping algorithms with different kernel functions could provide a better mapping to the human vision system.

### Chapter 6: Conclusion and Future Work

In this thesis, I have presented the kernel log-polar mapping model, user studies for finding the best parameters, as well as a GPU-based implementation and quantitative evaluation of the kernel foveated rendering pipeline. My research in this thesis has been published in a peer-reviewed journal [63] and I presented it at *ACM SIGGRAPH Symposium on Interactive 3D Graphics and Games* held during May 15 - 18, 2018 in Montreal, Canada.

First, I systematically vary the sampling rate and sampling distribution to better mimic the distribution of photo-receptors in the human vision system by embedding the polynomial kernel functions in the classic log-polar mapping. Second, I have carried out user studies, including a pilot study and a final one, in virtual reality HMD with integrated eye tracking to determine the best parameters for KFR. Finally, I evaluate the KFR pipeline through a quantitative evaluation with physically-based deferred-rendering scenes and ray-marching scenes. I have observed that the algorithm achieves a speedup of 3.2X for the procedural rendering scenes with ray-marched primitives and 2.8X for the physically-based deferred-rendering scenes.

With high frame rates, the KFR pipeline allows rendering more complex shaders

(e.g., real-time global illumination and physically-based rendering [64]) in real time, thus bringing higher power efficiency and better user experience for 3D games and other interactive visual computing applications. The work presented in this thesis is the first step towards kernel foreated rendering.

In future, I would like to apply the algorithm for interactively testing highfidelity path-tracing algorithms with the state-of-art noise reduction algorithms [43, 65,66]. Considering that current consumer HMDs have lens distortions [67], I also plan to explore warping from LP-buffer to "lens undistorted" image directly in order to provide substantial performance improvements.

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